

**Exercise 5: Error Propagation**  
**Due Tuesday, March 31**

The radii of most stars are too small to be resolved with direct images. The usual method for “measuring” stellar radii is to derive them from the Stefan-Boltzmann relation for thermal emission,

$$L = 4 \pi R^2 \sigma_{\text{SB}} T^4$$

...since  $L$  and  $T$  are easier to measure directly than  $R$ .

Given:

Property	Value
$T_{\text{eff}}$ for Star 337	$5000 \pm 100$ K
$L$ for Star 337	$4.0 \pm 0.1 \times 10^{33}$ ergs
$\sigma_{\text{SB}}$	$5.6 \times 10^{-5}$ erg cm <sup>-2</sup> K <sup>-4</sup> s <sup>-1</sup>
1 $R_{\text{sun}}$	$6.960 \times 10^{10}$ cm

Find and report:

1. the radius  $R$  for Star 337, in both cm and solar units;
2. the error  $\sigma_R$  for the radius of Star 337, in both cm and solar units; and
3. the percentage error of the radius of Star 337. Also,
4. indicate which term dominates the uncertainty.

Be sure to show:

- The applicable formulae for error propagation
- The derivation for the functional form of  $\sigma_R$
- The values (and units) of all key steps in the derivation